## A Method of measuring the specific heat of metals by rapio heating

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Zhurnal Prikladnoi Mekhaniki i Tekhnicheskoi Fiziki, Vol. 8, No. 4, pp. 141-143, 1967

The majority of existing methods of measuring the specific heat athigh temperatures require that the material being investigated be held at elevated temperatures for a comparatively long period. Hence difficulties arise in the study of materials whose properties may undergo change with time (recrystallization, allotropic changes, etc.) by existing methods other than impulse methods [1]. A description is given below of a method of measuring the specific heat of metals by heating them rapidly over a wide temperature range, so that the metal under investigation is at high temperature for only a comparatively short time. The specimen, in the form of a fine wire in a vacuum, is heated by passing an electric current through it. The heat liberated goes intoheating the wire, and there is some loss by thermal conduction through the ends and by radiation from the surface. With increase in the rate of heating, the proportion of the heat lost from the surface and through the ends diminishes in comparison with the amount that goes into heating the wire.

A theoretical evaluation of the method shows that the heat losses can in practice be neglected over the whole range of heating from room temperature to $1500^{\circ} \mathrm{C}$ if a wire about 200 mm long is heated at a rate on the order of tens of thousands of degrees per second. In this case all of the heat liberated goes into heating the specimen, and the specific heat may be determined from the formula

$$
\begin{equation*}
c_{p}=\frac{Q}{m d T / d \tau} \tag{1}
\end{equation*}
$$

Here $Q$ is the thermal energy liberated in the wire, $m$ is the mass of wire, and $T$ is the temperature.

By measuring the temperature variation with the time and also the thermal energy Q and calculating $\mathrm{dT} / \mathrm{d} T$, it is possible to determine the specific heat.

For this purpose the experimental setup shown diagrammatically in Fig. 1 was used; here 1 is the specimen, 2 is a time relay, 3 in an amplifier, 4 is a Schmitt trigger, 5 is a time-measuring device 6 is a potentiometer, 7 is a rapid-action switch, and 8 and 9 are two-way switches.

The filament 1 being investigated, with the resistance $R$ joined in series, is connected to a dc source by the rapid-action switch 7 . As a result, the filament is heated up, its resistance increases, and consequently the potential drop at it varies with time. Tomeasure the time dependence of this potential, one measures the time from the start of heating to the attainment of a definite potential level at the wire. By repeatedly heating the wire at various levels, the dependence can thus be determined. The level is set by an auxiliary circuit (source $E_{2}$, resistances $R_{1}, R_{2}, R_{N}$ ) and is equal to the potential drop at the resistance $\mathrm{R}_{1}$. The potential difference at the filament being investigated and the resistance $R_{1}$ supplies the inpur to the threshold circuit consisting of the wide-band dc amplifier 3 and the Schmitt trigger 4. At the instant when the heating of the wire is begun by a pulse from the contact 7 , the time-measuring device 5 is triggered.

The latter stops when the potential difference at the wire and the resistance $R_{1}$ is zero.


Fig. 1
The specific heat can be calculated from the measured time dependence of the potential at the wire. As can be seen from the dia-
gram, the thermal energy liberated in the wire is

$$
\begin{equation*}
Q==U\left(U_{1}-U\right)!R \tag{2}
\end{equation*}
$$

where $R$ also includes the internal resistance of the source $R_{i}$.


Fig. 2
The time dependence of the potential drop at the filament determines its rate of heating. The potential at the specimen is

$$
\begin{equation*}
U=l R_{T}\left(R \div-R_{T}\right) \tag{3}
\end{equation*}
$$

In Eq. (3) $E_{1}$ and $R$ are constants, while the resistance of the wire $\mathrm{R}_{\mathrm{T}}$ depends on its temperature T , which in turn varies with the time $\tau$, i. e. $U=U\left(R_{T}(T(\tau))\right)$. Differentiating $U$ with respect to $\tau$, we obtain

$$
\begin{gather*}
\frac{d V}{d \tau}==\frac{\partial U_{i}}{\partial R_{T}} \frac{d R_{T}}{d T} \frac{d T}{d \tau}= \\
=E_{I}\left\{\frac{1}{R+R_{T}}-\frac{R_{T}}{\left(R-R_{T}\right)^{2}}\right\} \frac{d R_{T}}{d T} \frac{d l^{\prime}}{d \tau}== \\
-\frac{R_{1} R}{\left(R+R_{T}\right)^{2}} \frac{d R_{T}}{d I} \frac{d T}{d \tau}, \tag{4}
\end{gather*}
$$

whence the rate of temperature change is

$$
\begin{equation*}
\frac{d T}{d \tau}=\frac{d U}{d \tau} \frac{\left(R_{T} \cdot R\right)^{2}}{\int R R_{0} \alpha} \quad\left(\alpha=\frac{1}{R_{0}} \cdot \frac{d R}{d T}\right) \tag{5}
\end{equation*}
$$

Here $\alpha$ is the temperature coefficient of resistance. By substituting Eqs. (2) and (5) in (1), we obtain the following formula for determining the specific heat:

$$
\begin{equation*}
r_{p}=\frac{R_{0}}{m R_{1} R^{2}} \frac{U(E-U)^{3}}{d U / d \tau} \alpha \tag{6}
\end{equation*}
$$

A platinum wire, 0.05 mm in diameter and $180-200 \mathrm{~mm}$ long, welded to special contacts on the holder, was chosen for the specificheat determination, After annealing to check the degree of purity of the metal, its resistance was measured at 0 and $100^{\circ} \mathrm{C}$, and the wire was installed in a vacuum chamber. The do source $\mathrm{E}_{1}$ consisted of an accumulator battery of 115 volts and a 0.6 -ohm internal resistance. The reactance-free $R$ varied from $20-60$ ohms in the experiments. In the rapid-action switch 7 one of the contacts consisted of a lead plate while the other was a copper rod with a pointed end. The switch completed the filament-heating circuit by the copper rod sharply striking the plate.

The resistances $R_{1}$ and $R_{2}$ are resistance boxes having a high degree of accuracy ( 0.02 ) and $\mathrm{R}_{\mathrm{N}}$ is a standard resistance coil of 100 ohms. The potentials $E_{1}$ and $U$ required in calculating the specific heat are measured by means of a dc potentiometer. The wideband dc amplifier 3 is the vertical-deflection amplifier of the S1-19A oscillograph. The output from the amplifier is connected to the Schmitt trigger, whose circuit is shown in Fig. 2. The trigger activates when the potential on the grid of the tube $L_{1}$ in-
creases until it becomes equal to the triggering threshold. A pulse is formed at the anode of the $L_{2}$ and this is fed to the grid of the cathode follower $L_{3}$. With the output from the latter the impulse is fed to the "stop" terminals of the time-measuring device 5 (Fig. 1), an F519 frequency meter with a resolving power of $1 \mu \mathrm{sec}$. To prevent the wire from becoming overheated, a time relay 2 is used which switches off the heat after a predetermined time.

The procedure for determining the specific heat is as follows: a definite potential level at $R_{1}$ is established by means of the resistances $R_{1}$ and $R_{2}$; the zero of the threshold circuit is fixed. For this purpose the amplifier input is short-circuited by the switch 8 , and operation of the trigger is achieved by regulating the "balance" of the


Fig. 3.
oscillograph. With a gain for the amplifier of about 1000 , the variation in the triggering threshold does not exceed 0.5 mV . After the zero has been fixed, switch 8 is changed over to the operating position and switch 7 is closed. At that instant (the beginning of heating) the time-measuring device is triggered by a pulse from the contact 7. When the wire reaches a predetermined temperature, the threshold circuit operates to stop the timing device 5 .

The readings of the timing device and the potentials $U$ and $E_{1}$ are recorded in a table of measurements. After this, $2-3$ minutes
are required for the wire to cool to its initial temperature, and during this time a new level of $U$ is established; then the zero of the threshold circuit is checked and the next measurement is taken and so on.

Differentiation of the potential/time function was carried out by the method of least squares.

In the experiments the rate of heating the specimens was varied by choosing different values of the resistance R from 6000 to $10^{5}$ $\mathrm{deg} / \mathrm{sec}$. It was found that at heating rates less then $20000 \mathrm{deg} / \mathrm{sec}$ the value calculated from Eq. (6) depends at high temperatures on the rate of heating; this is due to heat loss by heat conduction through the ends of the specimen. At higher rates of heating no dependence on the rate of heating was observed.

Measurements were made in the temperature range $400-1800^{\circ} \mathrm{K}$, but owing to the absence of reliable data for $\alpha$ at the higher temperatures the specific heat was calculated only up to $1470^{\circ} \mathrm{K}$.

The results of specific-heat measurements on platinum $C$ in $10^{3} \mathrm{~J} / \mathrm{kg}$ deg in the range $400-1470^{\circ} \mathrm{K}$, obtained at heating rates of 20000 to $10^{5} \mathrm{deg} / \mathrm{sec}$, are given in Fig. 3, in which the points indicate our data ( 1 is from [2] and 2 is from [3]). A preliminary estimate shows that the error in measuring the specific heat is about $3 \%$. Within the limits of accuracy of the method, the data obtained agree with those of other authors.

## REFERENCES

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